

# Strong Connectivity Strikes Back

Input file:            `standard input`  
Output file:          `standard output`  
Time limit:           1 second  
Memory limit:        512 megabytes

Vertices  $u$  and  $v$  of a directed graph are called strongly connected if there exists a path from  $u$  to  $v$  and a path from  $v$  to  $u$  in the graph. Note that if  $u$  and  $v$  are strongly connected, and  $v$  and  $w$  are strongly connected, then  $u$  and  $w$  are also strongly connected. Therefore, the vertices of the graph are divided into sets—strongly connected components. A vertex belonging to a strongly connected component is strongly connected to all vertices in the component (including itself) and is not strongly connected to any vertices outside the component.

During a graph class, Alice drew a directed graph with  $n$  vertices on the board and highlighted its strongly connected components. During the break, Bob decided to play a trick on Alice and erase the directions on some edges of the graph. He wants Alice to be able to uniquely restore the erased directions based on the remaining edges and the partition into strongly connected components after the break.

Help Bob by determining the maximum number of edges in the graph whose directions he can erase, as well as the number of ways he can do this.

More formally, find the maximum size of a subset of edges  $A$  that has the following property: if the directions of the edges in the set  $A$  are erased, then based on the information about the old strongly connected components and the directions of the edges not in the set  $A$ , the directions of the edges in the set  $A$  can be uniquely restored in such a way that the strongly connected components remain unchanged.

Since the number of such maximum subsets can be very large, output it modulo  $10^9 + 7$ .

Solutions that correctly determine the maximum size of the set  $A$  but incorrectly present the number of such subsets will receive partial points.

## Input

The first line contains three integers  $n$ ,  $m$ , and  $g$  ( $2 \leq n \leq 2000$ ,  $1 \leq m \leq 2000$ ,  $0 \leq g \leq 7$ )—the number of vertices and edges in the graph, respectively, as well as the test group number.

The next  $m$  lines contain two integers  $u_i$  and  $v_i$  ( $1 \leq u_i, v_i \leq n$ ,  $u_i \neq v_i$ )—the numbers of the vertices that are the start and end of the  $i$ -th edge.

It is guaranteed that for any  $1 \leq i, j \leq n$   $(u_i, v_i) \neq (u_j, v_j)$  and  $(u_i, v_i) \neq (v_j, u_j)$ , meaning that any two vertices are connected by at most one edge, regardless of direction.

## Output

In the first line, output a single number—the size of the maximum subset of edges whose directions can be erased.

In the second line, output a single number—the number of such subsets modulo  $10^9 + 7$ . If you do not want to present the number of such subsets, then in the second line, instead, output any number from  $-1$  to  $10^9 + 6$ . In this case, your solution will receive partial points for the test.

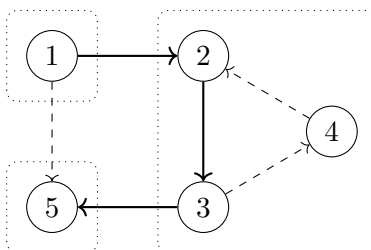
Note that omitting any number in the second line leads to a verdict of "Wrong Answer" and zero points for this test, regardless of the correctness of the size of the subset.

## Example

standard input	standard output
5 6 0	3
1 2	3
1 5	
2 3	
3 4	
3 5	
4 2	

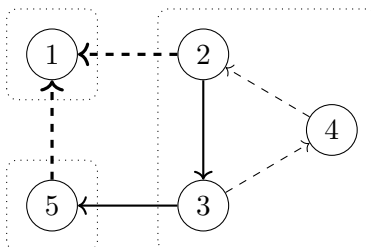
## Note

The graph from the example with strongly connected components highlighted:



The directions on the dashed edges can be removed. Indeed, the edge  $(1, 5)$  cannot be oriented in the opposite direction, because otherwise, vertices 1, 2, 3, and 5 would belong to the same strongly connected component. The edges  $(3, 4)$  and  $(4, 2)$  cannot be oriented differently either, because then vertices 2, 3, and 4 would not belong to the same strongly connected component.

Now, let's consider an incorrect way of selecting a subset of edges:



Here, the directions on the bold dashed edges cannot be removed. For example, if we reverse the orientation of edges  $(1, 2)$  and  $(1, 5)$ , we get a graph with the same decomposition into strongly connected components.

It can be shown that the directions on exactly 4 edges cannot be removed, so the answer is 3.

## Scoring

The tests for this problem consist of seven groups. The rules for scoring the subgroups are described below.

If the size of the maximum subset of edges whose directions can be erased and the number of such subsets are correctly calculated in all tests of the group, full points are awarded for the group.

Otherwise, if the size of the maximum subset of edges whose directions can be erased is correctly calculated in all tests of the group, but the number is incorrect in at least one test of the group, partial points are awarded for the group. Note that dependent groups will be tested in this case and may even be scored full points.

Group	Points		Additional Constraints		Required Groups	Comment
	Partial	Full	$n$	$m$		
0	0	0	–	–	–	Examples.
1	7	11	$n \leq 14$	$m \leq 14$	0	
2	5	9	$n \leq 20$	$m \leq 20$	0, 1	
3	8	12	–	–	–	$u_i < v_i$ , for all $1 \leq i \leq n - 1$ there is an edge $(i, i + 1)$
4	8	13	–	–	3	$u_i < v_i$
5	12	20	–	–	–	for all $1 \leq i \leq n - 1$ there is an edge $(i, i + 1)$ , there is an edge $(n, 1)$
6	13	21	–	–	5	the graph consists of one strongly connected component
7	8	14	–	–	0 – 6	